

SECTION A

[for correct attempt +1 each , for wrong attempt -1/4 for each]

1) The number of real roots of the equation $x^2 - 3|x| + 2 = 0$ is

- a) 2 b) 1 c) 4 d) 3

2) If $\log_2 (5 \times 2^x + 1)$, $\log_4 (2^{1-x} + 1)$ and 1 are in A.P., then x equals

- a) $\log_2 5$ b) $1 - \log_5 2$ c) $\log_5 2$ d) none of these

3) If $x = 1 + i$ is a root of the equation $x^3 - ix + 1 - i = 0$ then the other real root is

- a) 0 , b) 1 , c) -1 , d) none of these

4) The largest term common to the sequences 1, 11, 21, 31, ... to 100 terms and 31, 36, 41, 46, ... to 100 terms is

- a) 381 , b) 471 , c) 281 , d) none of these

5) If the $x^2 + 2(a + b + c)x + 3(bc + ab + ca)$ is a perfect square, then

- a) $a = b = c$, b) $a = \pm b = \pm c$, c) $a = b \neq c$, d) none of these

6) If a, b and c are in A.P. then $a^3 + c^3 - 8b^3$ is equal to

- a) $2abc$, b) $6abc$, c) $4abc$, d) none of these

7) Sum of the non real root of $(x^2 + x - 2)(x^2 + x - 3) = 12$ is

- a) -1 , b) 1 , c) -6 , d) 6

8) Consider an A.P. $a_1, a_2, a_3, \dots$ such that $a_3 + a_5 + a_8 = 11$ and $a_4 + a_2 = -2$, then the value of $a_1 + a_6 + a_7$ is

a) -8 , b)5 , c)7 , d)9

9) The number of irrational roots of the equation $\frac{4x}{(x^2+x+3)} + \frac{5x}{(x^2-5x+3)} = -\frac{3}{2}$ is

a)4 , b)0 , c)1 , d)2

10) Suppose that $F(n+1) = \frac{2F(n)+1}{2}$ for $n = 1, 2, 3, \dots$ and $F(1) = 2$, Then, $F(101)$ equals

a)50 , b)52 , c)54 , d)none of these

11) If $\tan^2 \frac{\pi-A}{4} + \tan^2 \frac{\pi-B}{4} + \tan^2 \frac{\pi-C}{4} = 1$, then ΔABC is

a)equilateral , b)isosceles , c)scalene , d)none of these

12) A quadratic equation whose product of roots x_1 and x_2 is equal to 4 and satisfying

the relation $\frac{x_1}{x_1-1} + \frac{x_2}{x_2-1} = 2$ is

a) $x^2 - 2x + 4 = 0$, b) $x^2 + 2x + 4 = 0$
c) $x^2 + 4x + 4 = 0$, d) $x^2 - 4x + 4 = 0$

13) Three numbers form an increasing G.P. If the middle number is doubled, then the new numbers are in A.P. The common ratio of the G.P. is

a) $2 - \sqrt{3}$, b) $2 + \sqrt{3}$, c) $\sqrt{3} - 2$, d) $3 + \sqrt{2}$

14) If the roots of the equation $(a-1)(x^2+x+1)^2 = (a+1)(x^4+x^2+1)$ are real and distinct then the value of $a \in$

a) $(-\infty, 3]$, b) $(-\infty, -2) \cup (2, \infty)$, c) $[-2, 2]$, d) $[-3, \infty)$

15) If x, y, z are in G.P. and $a^x = b^y = c^z$, then

a) $\log_b a = \log_a c$, b) $\log_c b = \log_a c$
c) $\log_c b = \log_b a$, d) none of these

16) If α, β are real and α^2, β^2 are the roots of the equation $a^2 x^2 + x + 1 - a^2 = 0$ ($a > 1$), then $\beta^2 =$

a) a^2 , b) $1 - \frac{1}{a^2}$, c) $1 - a^2$, d) $1 + a^2$

17) If x , $2x + 2$ and $3x + 3$ are first three terms of a G.P., then the fourth term is

a) 27 , b) -27 , c) 13.5 , d) -13.5

18) The value of m for which one of the roots of $x^2 - 3x + 2m = 0$ is double of one of the roots of $x^2 - x + m = 0$ is

a) -2 , b) 1 , c) 2 , d) none of these

19) If a, b and c are in A.P. and $b - a, c - b$, and a are in G.P., then $a : b : c$ is

a) 1:2:3 , b) 1:3:5 , c) 2:3:4 , d) 1:2:4

20) If α, β, γ are the roots of $x^3 - x^2 - 1 = 0$ then the value of $\frac{1+\alpha}{1-\alpha} + \frac{1+\beta}{1-\beta} + \frac{1+\gamma}{1-\gamma}$ is equal to

a) -5 , b) -6 , c) -7 , d) -2

21) $a, b, c, d \in \mathbb{R}^+$ such that a, b and c are in A.P. and b, c and d are in H.P. then

a) $ab = cd$, b) $ac = bd$, c) $bc = ad$, d) none of these

22) In a ΔABC , the internal angle bisector of $\angle ABC$ meets AC at K . If

$BC = 2, CK = 1$ and $BK = \frac{3\sqrt{2}}{2}$, then find the length of side AB

a) 1 , b) 2 , c) 3 , d) 4

23) If x is real, then the maximum value of $\frac{3x^2 + 9x + 17}{3x^2 + 9x + 7}$ is

a) $\frac{1}{4}$, b) 41 , c) 1 , d) $\frac{17}{7}$

24) The 15th term of the series $2\frac{1}{2} + 1\frac{7}{13} + 1\frac{1}{9} + \frac{20}{23} + \dots$ is

a) $\frac{10}{39}$, b) $\frac{10}{21}$, c) $\frac{10}{23}$, d) none of these

25) For $x^2 - (a + 3)|x| + 4 = 0$ to have real solutions, the range of a is

a) $(-\infty, -7] \cup [1, \infty)$, b) $(-3, \infty)$, c) $(-\infty, -7]$, d) $[1, \infty)$

26) The sum of $i - 2 - 3i + 4 \dots$ upto 100 terms where $i = \sqrt{-1}$ is

a) $50(1 - i)$, b) $25i$, c) $25(1 + i)$, d) $100(1 - i)$

27) Let x, y, z, t be real numbers $x^2 + y^2 = 9, z^2 + t^2 = 4$ and $xt - yz = 6$.
Then the greatest value of $P = xz$ is

a) 2 , b) 3 , c) 4 , d) 6

28) Let T_r and S_r be the r^{th} term and sum upto r^{th} of a series respectively.
If for an odd number $n, S_n = n$ and $T_n = \frac{T_{n-1}}{n^2}$ then T_m (m being even) is

a) $\frac{2}{1 + m^2}$, b) $\frac{2m^2}{1 + m^2}$, c) $\frac{(m + 1)^2}{2 + (m + 1)^2}$, d) $\frac{2(m + 1)^2}{1 + (m + 1)^2}$

29) The number of integral values of x satisfying
 $\sqrt{-x^2 + 10x - 16} < x - 2$ is

a) 0 , b) 1 , c) 2 , d) 3

30) The sum of the series $\frac{x}{1 - x^2} + \frac{x^2}{1 - x^4} + \frac{x^4}{1 - x^8} + \dots$ to infinite terms
if $|x| < 1$, is

a) $\frac{x}{1 - x}$, b) $\frac{1}{1 - x}$, c) $\frac{1 + x}{1 - x}$, d) 1

31) If $x^2 + ax - 3x - (a + 2) = 0$ has real and distinct roots then, minimum
value of $\frac{a^2 + 1}{a^2 + 2}$ is

a) 1 , b) 0 , c) $\frac{1}{2}$, d) $\frac{1}{4}$

32) If x, y, z are real and $4x^2 + 9y^2 + 16z^2 - 6xy - 12yz - 8zx = 0$ then x, y, z are in

a) A.P. , b) G.P. , c) H.P. , d) none of these

33) Consider a ΔABC and let a, b and c denote the lengths of the sides opposite to the vertices A, B and C , respectively. Suppose $a = 2, b = 3, c = 4$ and H be the orthocentre. Find $15(HA)^2$.

a) 256 , b) 146 , c) 196 , d) 216

34) the value of the expression $x^4 - 8x^3 + 18x^2 - 8x + 2$ when $x = 2 + \sqrt{3}$

a) 2 , b) 1 , c) 0 , d) 3

35) The sum of the series $a - (a + d) + (a + 2d) - (a + 3d) + \dots$ upto $(2n + 1)$ terms is

a) $-nd$, b) $a + 2nd$, c) $a + nd$, d) $2nd$

36) The set of all possible real values of a such that the inequality $(x - (a - 1))(x - (a^2 + 2)) < 0$ holds for all $x \in (-1, 3)$ is

a) $(0, 1)$, b) $(\infty, -1]$, c) $(-\infty, -1)$, d) $(1, \infty)$

37) Let $[t_n]$ be a sequence of integers in G.P. in which $t_4 : t_6 = 1 : 4$ and $t_2 + t_5 = 216$. Then t_1 is

a) 12 , b) 14 , c) 16 , d) none of these

38) If a, b and c are real numbers such that $a^2 + b^2 + c^2 = 1$, then $ab + bc + ca$ lies in the interval

a) $\left[\frac{1}{2}, 2\right]$, b) $[-1, 2]$, c) $\left[-\frac{1}{2}, 1\right]$, d) $[-1, 1/2]$

39) If $a, \frac{1}{b}, c$ and $\frac{1}{p}, q, \frac{1}{r}$ form two arithmetic progression of the same common difference, then a, q, c are in A.P. if

a) p, b, r are in A.P. , b) $\frac{1}{p}, \frac{1}{b}, \frac{1}{r}$ are in A.P. , c) p, b, r are in G.P. , d) none of these

40) x_1 and x_2 are the roots of $ax^2 + bx + c = 0$ and $x_1x_2 < 0$. Roots of $x_1(x - x_2)^2 + x_2(x - x_1)^2 = 0$ are

a) real and opposite sign , b) negative , c) positive , d) non real

41) If a, x and b are in A.P., a, y and b are in G.P. and a, z, b are in H.P. such that $x = 9z$ and $a > 0, b > 0$, then

a) $|y| = 3z$, b) $x = 3|y|$, c) $2y = x + z$, d) none of these

42) If α, β be the roots of the equation $(x - a)(x - b) + c = 0$ ($c \neq 0$), then the roots of the equation $(x - c - \alpha)(x - c - \beta) = c$ are

a) $a + c$ and $b + c$, b) $a - c$ and $b - c$, c) a and $b + c$, d) $a + c$ and b

43) In ΔABC , if $\cos A + \sin A - \frac{2}{\cos B + \sin B} = 0$, then $\frac{a + b}{c}$ is equal to

a) $\sqrt{2}$, b) 1 , d) $2\sqrt{2}$, c) $\frac{1}{\sqrt{2}}$

44) The 15th term of the series $2\frac{1}{2} + 1\frac{7}{13} + 1\frac{1}{9} + \frac{20}{23} + \dots$ is

a) $\frac{10}{39}$, b) $\frac{10}{21}$, c) $\frac{10}{23}$, d) none of these

45) The coefficient of x in the equation $x^2 + px + q = 0$ was wrongly written as 17 in place of 13 and the roots thus found was -2 and -15 . Then the roots of the correct equation are

a) $-3, 10$, b) $-3, -10$, c) $3, -10$, d) none of these

46) If α, β be the roots of the equation $2x^2 - 35x + 2 = 0$, then the value of $(2\alpha - 35)^3(2\beta - 35)^3$ is equal to

a) 8 , b) 1 , c) 64 , d) none of these

47) consider a ΔABC and let a, b and c denote the lengths of the side opposite to vertices A, B and C , respectively. If $a = 1, b = 3$ and $c = 60^\circ$, then $\sin^2 B$ is equal

a) $\frac{27}{28}$, b) $\frac{3}{28}$, c) $\frac{81}{28}$, d) $\frac{1}{3}$

48) The least value of the expression $x^2 + 4y^2 + 3z^2 - 2x - 12y - 6z + 14$ is

a) 1 , b) no least value , c) 0 , d) none of these

49) Let $S = \frac{4}{19} + \frac{4}{19^2} + \frac{4}{19^3} + \dots$ upto ∞ . Then S is equal to

a) $\frac{40}{9}$, b) $\frac{38}{81}$, c) $\frac{36}{171}$, d) none of these

50) The number of roots of the equation $\sqrt{x-2}(x^2 - 4x + 3) = 0$ is

a) three , b) four , c) one , d) two

SECTION B

[FOR CORRECT ATTEMPT +2 EACH , FOR WRONG ATTEMPT -1/2 EACH]

51) In ΔABC , let $b = 6$, $c = 10$ and $r_1 = r_2 + r_3 + r$ then find the area of ΔABC

a) 25 , b) 30 , c) 70 , d) 55

52) Let a, b and c be real numbers such that $4a + 2b + c = 0$ and $ab > 0$. Then the equation $ax^2 + bx + c = 0$ has

a) complex roots , b) exactly one root , c) real roots , d) none of these

53) The value of $0.2^{\log_{\sqrt{5}}(\frac{1}{4} + \frac{1}{8} + \frac{1}{16} + \dots)}$ is

a) 4 , b) $\log 4$, c) $\log 2$, d) none of these

54) If α, β are the roots of the equation $x^2 - 2x + 3 = 0$. Then the equation whose roots are $P = \alpha^3 - 3\alpha^2 + 5\alpha - 2$ and $Q = \beta^3 - \beta^2 + \beta + 5$ is

a) $x^2 + 3x + 2 = 0$, b) $x^2 - 3x - 2 = 0$, c) $x^2 - 3x + 2 = 0$, d) none of these

55) If S_n denotes the sum of first 'n' terms of an A.P. and $\frac{S_{3n} - S_{n-1}}{S_{2n} - S_{2n-1}} = 31$, then the value of n is

a) 21 , b) 15 , c) 16 , d) 19

56) If $X = 2 + 2^{2/3} + 2^{1/3}$, then the value of $x^3 - 6x^2 + 6x$ is

a) 3 , b) 2 , c) 1 , d) -2

57) If the p^{th} , q^{th} , r^{th} and s^{th} term of an A.P. are in G.P. then $p - q, q - r, r - s$ are in

a) A.P. , b) G.P. , c) H.P. . d) none of these

58) If α, β are the roots of $ax^2 + c = bx$, then the equation $(a + cy)^2 = b^2y$ in y has the roots

a) $\alpha\beta^{-1}, \alpha^{-1}\beta$, b) α^{-2}, β^{-2} , c) α^{-1}, β^{-1} , d) α^2, β^2

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59) Sum of three numbers in G.P. be 14. If one is added to first and second and 1 is subtracted from the third, the new numbers are in A.P. The smallest of them is

a) 2 , b) 4 , c) 6 , d) 10

60) If α, β are the roots of the equation $ax^2 + bx + c = 0$, and $\alpha + h, \beta + h$ are the roots of the $px^2 + qx + r = 0$, then h is

a) $-\frac{1}{2}\left(\frac{a}{b}-\frac{p}{q}\right)$, b) $\left(\frac{b}{a}-\frac{q}{p}\right)$, c) $1/2(b/a - q/p)$, d) none of these

61) If $\frac{1}{1^2} + \frac{1}{2^2} + \frac{1}{3^2} + \dots \infty = \frac{\pi^2}{6}$, then $\frac{1}{1^2} + \frac{1}{3^2} + \frac{1}{5^2} + \dots$ equals

a) $\frac{\pi^2}{8}$, b) $\frac{\pi^2}{12}$, c) $\frac{\pi^2}{3}$, d) $\frac{\pi^2}{2}$

62) If roots of $x^2 - (a - 3)x + a = 0$, are such that at least one of them is greater than 2 , then

a) $a \in [7, 9]$, b) $a \in [7, \infty)$, c) $a \in [9, \infty)$, d) $a \in [7, 9)$

63) If α, β, γ and σ are the roots of the equation $x^4 + 4x^3 - 6x^2 + 7x - 9 = 0$, then the value of $(1 + \alpha^2)(1 + \beta^2)(1 + \gamma^2)(1 + \sigma^2)$ is

a) 9 , b) 11 , c) 13 , d) 5

64) The sum of 20 terms of a series of which every term is 2 times the term before it, and every odd term is 3 times the term before it , the first term being unity is

a) $\left(\frac{2}{7}\right)(6^{10} - 1)$, b) $\left(\frac{3}{7}\right)(6^{10} - 1)$, c) $\left(\frac{3}{5}\right)(6^{10} - 1)$, d) none of these

65) If α, β, γ are such that $\alpha + \beta + \gamma = 2$, $\alpha^2 + \beta^2 + \gamma^2 = 6$, $\alpha^3 + \beta^3 + \gamma^3 = 8$, then $\alpha^4 + \beta^4 + \gamma^4$ is equal to

a) 18 , b) 10 , c) 15 , d) 36

SECTION C

[FOR CORRECT ATTEMPT +2 EACH , FOR WRONG ATTEMPT 0 EACH]

66) The value of x satisfying the equation $2^{2x} - 8 \times 2^x = -12$ is

a) $1 + \frac{\log 3}{\log 2}$, b) $\frac{1}{2} \log 6$, c) $1 + \log \frac{3}{2}$, d) 1

67) $\frac{1}{\sqrt{2} + \sqrt{5}} + \frac{1}{\sqrt{5} + \sqrt{8}} + \frac{1}{\sqrt{8} + \sqrt{11}} + \dots n \text{ terms}$ is equal to

a) $\frac{\sqrt{3n+2} - \sqrt{2}}{3}$, b) $\frac{n}{\sqrt{2+3n} + \sqrt{2}}$, c) less than n , d) less than $\sqrt{\frac{n}{3}}$

68) If the equations $4x^2 - x - 1 = 0$, and $3x^2 + (\mu + \rho)x + \rho - \mu = 0$ have a root common then the rational values of ρ and μ are

a) $\rho = -\frac{3}{4}$, b) $\rho = 0$, c) $\mu = 3/4$, d) $\mu = 0$

69) If p, q, r are in A.P., then which of this is true

- a) p^{th}, q^{th}, r^{th} term of an A.P., are in A.P. , b) p^{th}, q^{th}, r^{th} term of a H.P. are in H.P.
c) p^{th}, q^{th}, r^{th} term of a G.P. are in G.P. , d) none of these

70) If the equations $x^2 + bx - a = 0$ and $x^2 - ax + b = 0$ have a common root then

a) $a + b = 0$, b) $a = b$, c) $a - b = 1$, d) $a + b = 1$

71) For an increasing A.P. $a_1, a_2, a_3, \dots, a_n$ if $a_1 + a_3 + a_5 = -12$ and $a_1 a_3 a_5 = 80$ then which of the following is/are true

a) $a_1 = -10$, b) $a_2 = -1$, c) $a_3 = -4$, d) $a_5 = +2$

72) If $x^3 + 3x^2 - 9x + c$ is of the form $(x - \alpha)^2(x - \beta)$, then c is equal to

a) 27 , b) -27 , c) 5 , d) -5

73) The next term of the G.P. $x, x^2 + 2$ and $x^3 + 10$ is

a) $\frac{729}{16}$, b) 6 , c) 0 , d) 54

74) If a, b, c are in G.P. then the roots of the equation $ax^2 + bx + c = 0$ are in the ratio

a) $\frac{1}{2}(-1 + i\sqrt{3})$, b) $\frac{1}{2}(1 - i\sqrt{3})$, c) $\frac{1}{2}(-1 - i\sqrt{3})$, d) $\frac{1}{2}(1 + i\sqrt{3})$

75) If $\frac{1}{b-a} + \frac{1}{b-c} = \frac{1}{a} + \frac{1}{c}$ then

a) a, b, c are in H.P. , b) a, b, c are in G.P. , c) $b = a + c$, d) $3a = b + c$